

Multimodal Deep Learning



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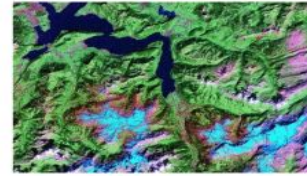
- Introduction
- Challenges
 - Representation
 - Translation
 - Alignment
 - Fusion
 - Co-Learning
- Interpretability in Multimodal Deep Learning



Aim of the presentation

- Identify challenges particular to Multimodal Learning
- Popular research topics in the field
- Brief of the problem I have been working on - Interpretability in Multimodal Deep Learning

Multimodal Learning - Heterogeneous Information Sources

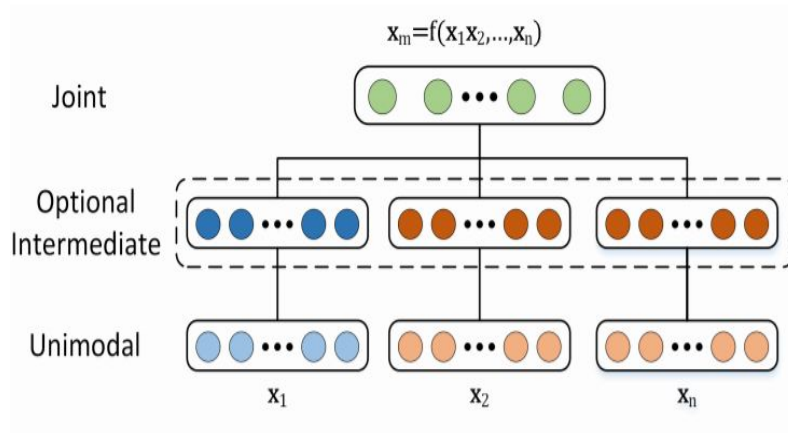




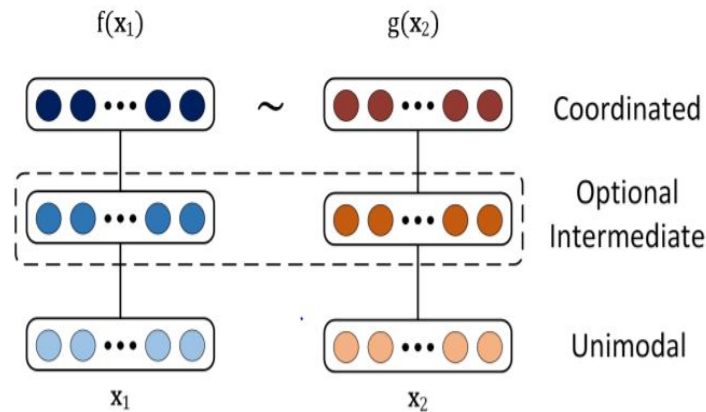
Challenge - 1) Representation

- How to combine the information from multiple sources?
- How to deal with different levels of noise?
- How to deal with missing data?

1) Representation - Ways of learning



(a) Joint representation

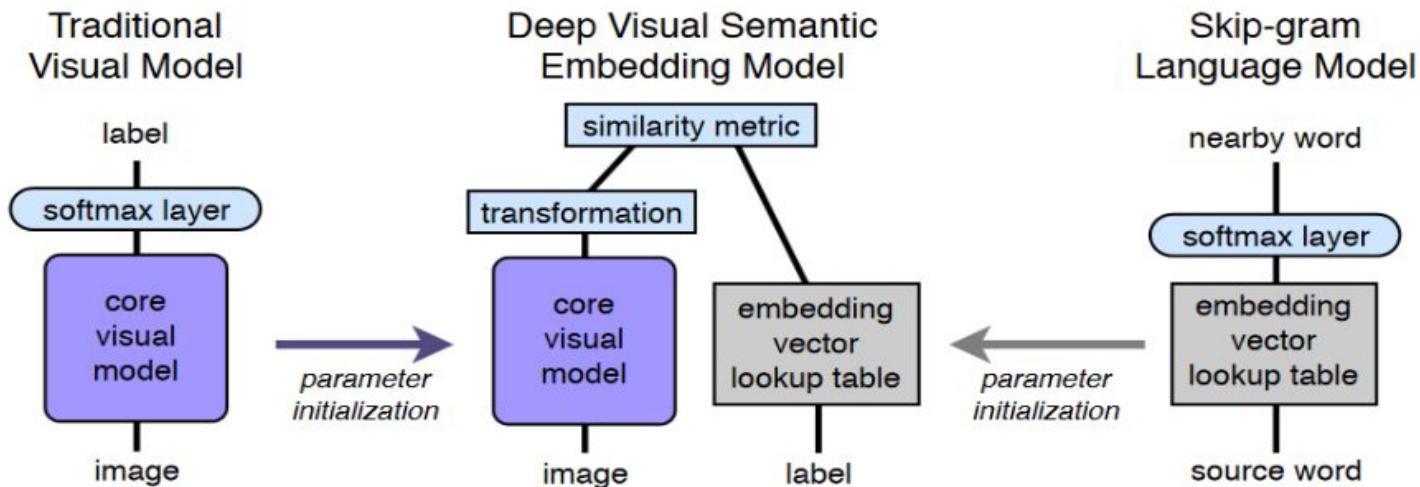


(b) Coordinated representations



Coordinated Representation

DeViSE — a deep visual-semantic embedding - Similarity model





Challenge - 2) Translation

{...a **multicolored table** in the middle of the room...,
...four red and white chairs and a **colorful table**, ...}

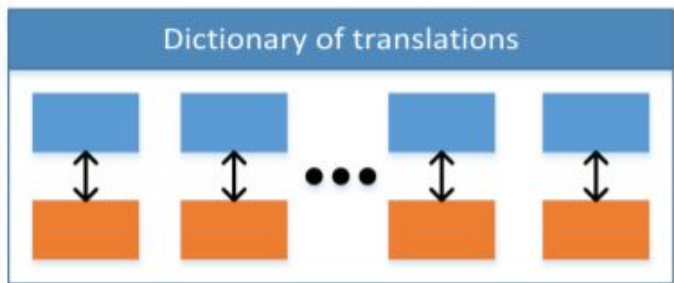


{...**L-shaped room** with walls that have 2 tones of gray...,
A **dark room** with a pool table...}

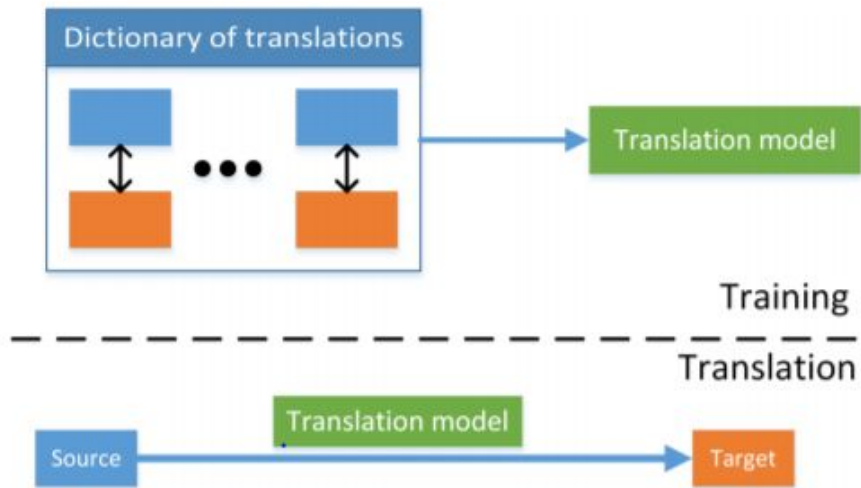




Translation



(a) Example-based



(b) Generative

How to evaluate translations



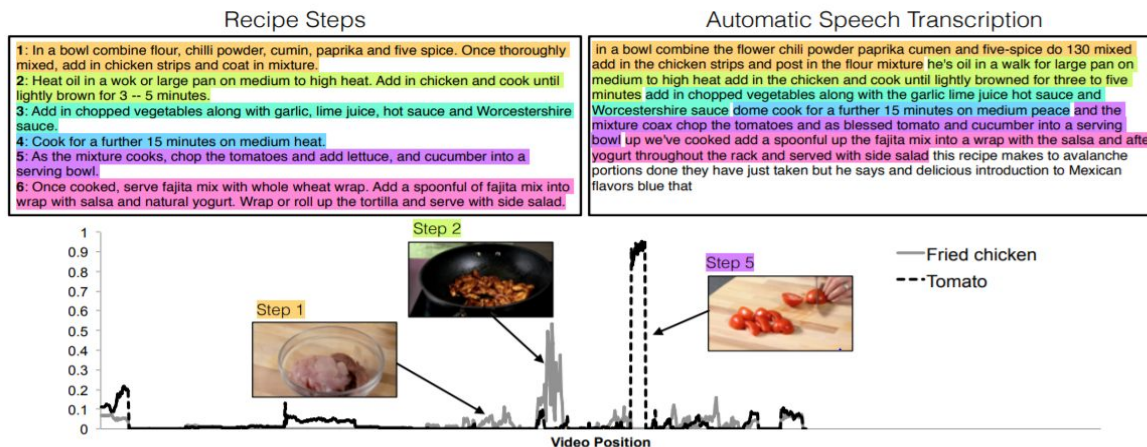
Candidate: Football players gathering to contest something to collaborating officials.

Reference: A football player in red and white is holding both hands up.



Challenge - 3) Alignment

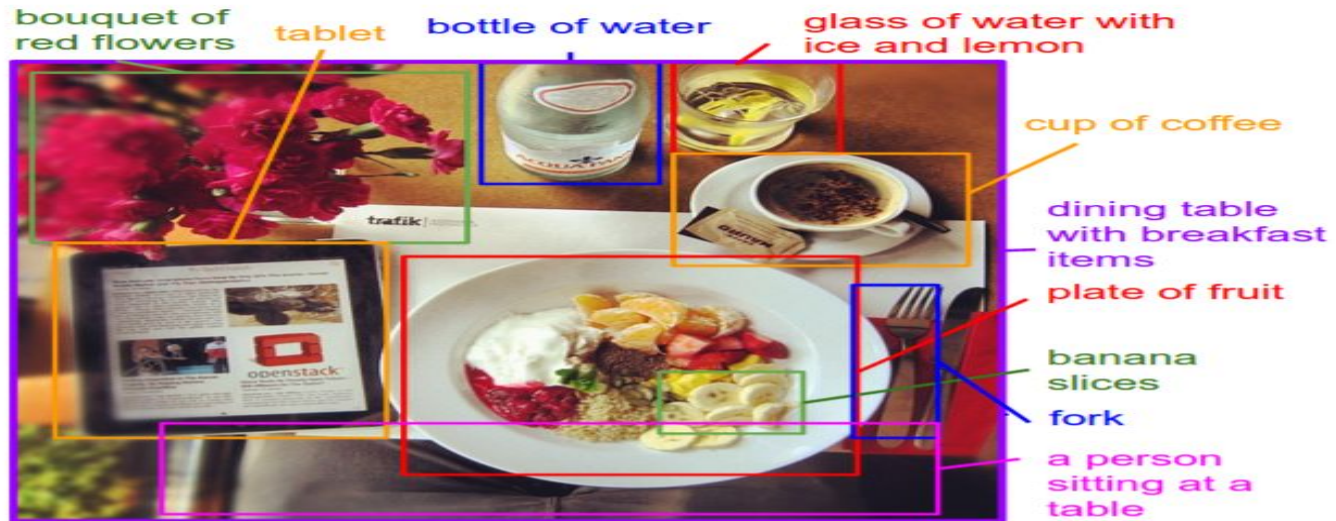
- 1) Identify the direct relations between (sub)elements from two or more different modalities.





Alignment

Given an image and a caption we want to find the areas of the image corresponding to the caption's words or phrases

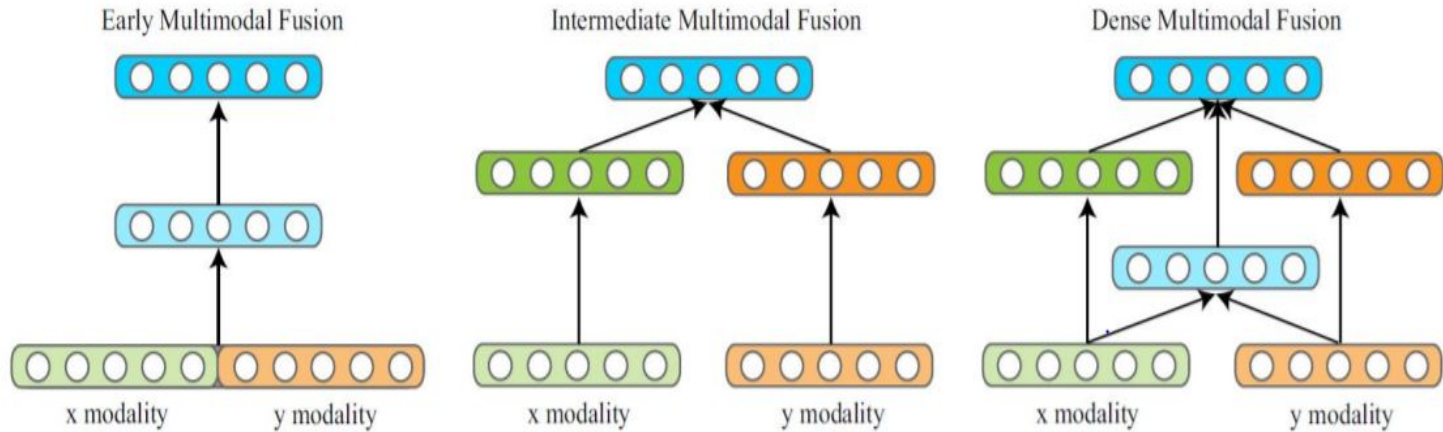




Alignment problems

- Few datasets with explicitly annotated alignments
- It is difficult to design similarity metrics between modalities
- Existence of multiple possible alignments and not all elements in one modality have correspondences in another

Challenge - 4) Fusion





Fusion

- Signals not temporarily aligned
- Lack of interpretability of where is the prediction coming from
 - (This is what I am working on)



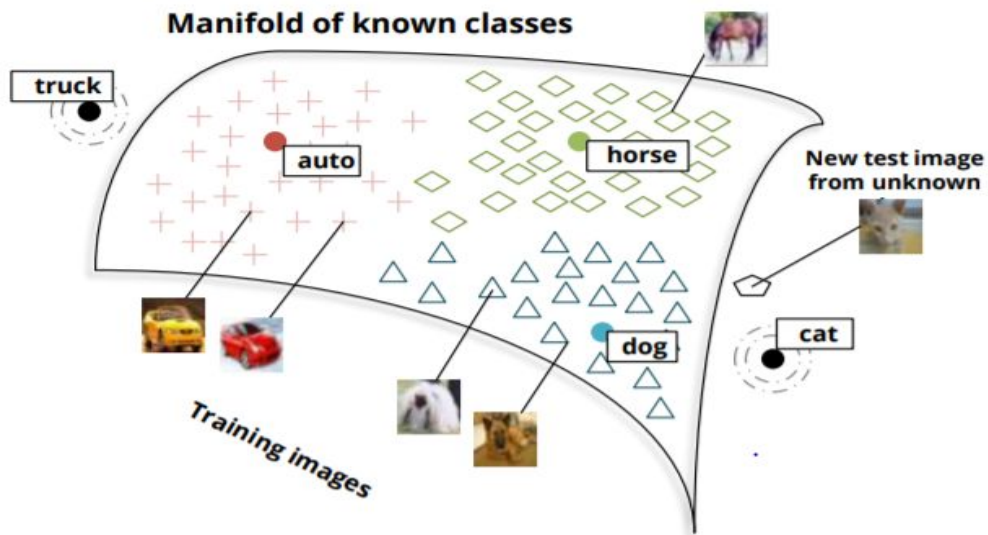
Challenge - 5) Co-Learning

- Aiding the modeling of a (resource poor) modality by exploiting knowledge from another (resource rich) modality.
- When one modality has lack of annotated data, noisy inputs and unreliable labels.



Colearning - Zero Shot learning

Using text embeddings to classify unseen classes of images





Interpretability in Multimodal Deep Learning

Problem statement -

Not every modality has **equal contribution** to the prediction

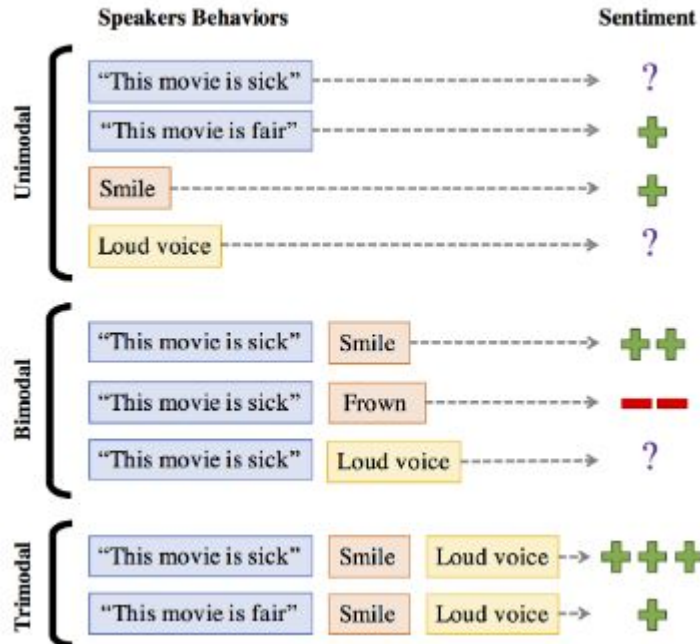


Interpretability in Multimodal Deep Learning

Solution -

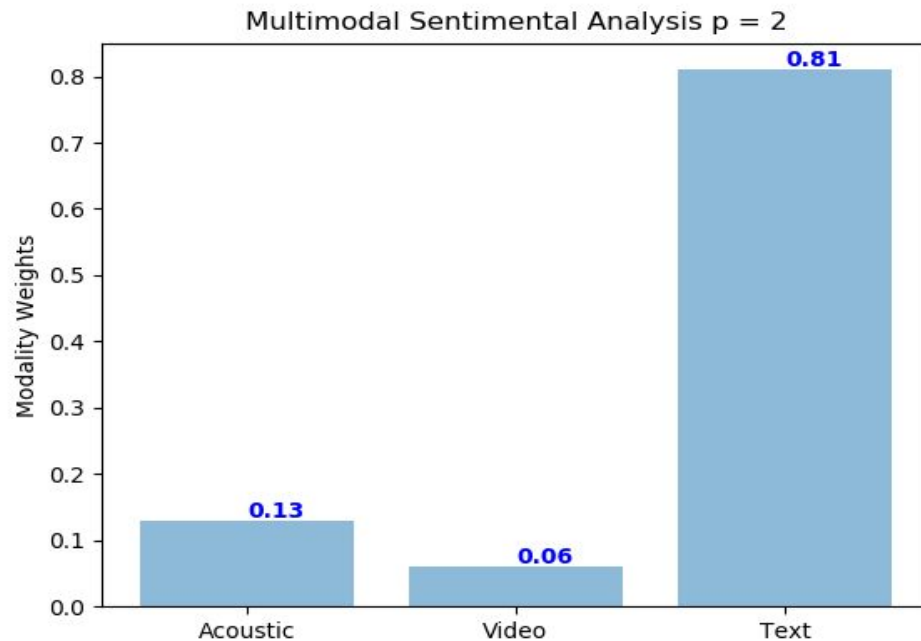
We give **different weights** to different modalities

Real data experiments - Multimodal Sentiment Analysis(MOSI Dataset)

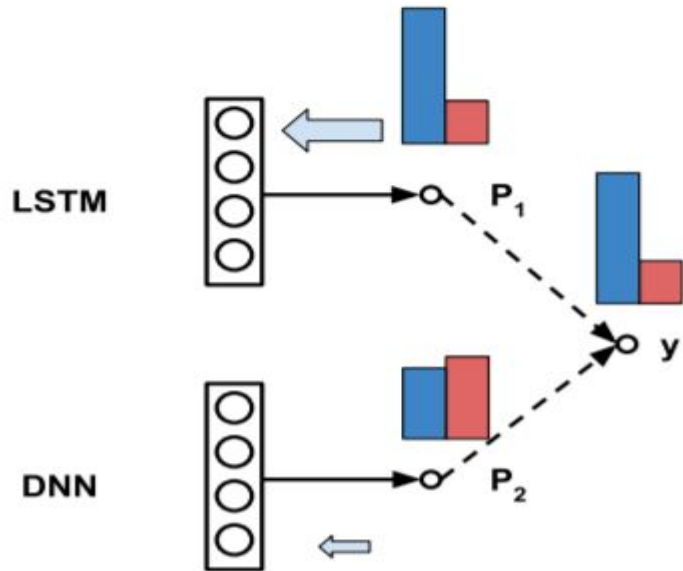




Multimodal Sentiment Analysis



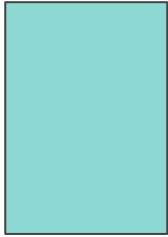
P1 and P2 contribution of each modality



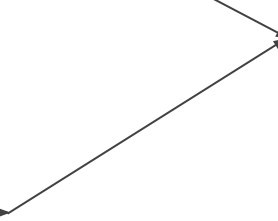
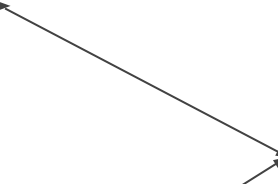
$$N_p = \sum_{m=1}^M p_m \langle f_{w_1^m, w_2^m \dots w_{L-1}^m}^m(x), W_L^m \rangle + b$$



Θ



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Modified loss function with β weight given to each modality

$$\min_{\substack{w_1, w_2, \dots, w_L, \beta \\ \beta \in \mathbf{R}^M, \beta \geq 0, \|\beta\|_p \leq 1}} \left(\sum_{i=1}^n \ell \left(\sum_{m=1}^M \sqrt{\beta_m} \langle w_L^m, f^m(x_i^m) \rangle + b, y_i \right) + \Lambda \sum_{l=1}^L \sum_{m=1}^M \|w_l^m\|_2^2 \right)$$

Modified loss function with β weight given to each modality

$$\min_{\substack{w_1, w_2, \dots, w_L, \beta \\ \beta \in \mathbf{R}^M, \beta \geq 0, \|\beta\|_p \leq 1}} \left(\sum_{i=1}^n \ell \left(\sum_{m=1}^M \sqrt{\beta_m} \langle w_L^m, f^m(x_i^m) \rangle + b, y_i \right) + \Lambda \sum_{l=1}^L \sum_{m=1}^M \|w_l^m\|_2^2 \right)$$

$$w_L^m \leftarrow \sqrt{\beta_m} w_L^m,$$

Let's make β trainable

$$\min_{\substack{w_1, w_2, \dots, w_L, \beta \\ \beta \in \mathbf{R}^M, \beta \geq 0, \|\beta\|_p \leq 1}} \sum_{i=1}^n \ell \left(\sum_{m=1}^M \langle w_L^m, f_{w_1^m, w_2^m, \dots, w_{L-1}^m}(x_i^m) \rangle + b, y_i \right) + \Lambda \sum_{l=1}^{L-1} \sum_{m=1}^M \|w_l^m\|_2^2 + \Lambda \sum_{m=1}^M \frac{\|w_L^m\|_2^2}{\beta_m}.$$

Modified loss function with β weight given to each modality

$$\min_{\substack{w_1, w_2, \dots, w_L, \beta \\ l \in \mathbb{R}^M, \beta \geq 0, \|\beta\|_p \leq 1}} \sum_{i=1}^n \ell \left(\sum_{m=1}^M \langle w_L^m, f_{w_1^m, w_2^m, \dots, w_{L-1}^m}^m(x_i^m) \rangle + b, y_i \right) + \Lambda \sum_{l=1}^{L-1} \sum_{m=1}^M \|w_l^m\|_2^2 + \Lambda \sum_{m=1}^M \frac{\|w_L^m\|_2^2}{\beta_m}.$$

Using the Lemma

$$\min_{\beta > 0, \|\beta\|_p \leq 1} \sum_{m=1}^M \frac{A_m}{\beta_m} = \left(\sum_{m=1}^M A_m^{\frac{p}{p+1}} \right)^{\frac{p+1}{p}}$$

$$\min_{w_1, w_2, \dots, w_L} \sum_{i=1}^n \ell \left(\sum_{m=1}^M \langle w_L^m, f^m(x_i^m) \rangle + b, y_i \right) + \Lambda \sum_{l=1}^{L-1} \sum_{m=1}^M \|w_l^m\|_2^2 + \Lambda \left(\sum_{m=1}^M \|w_L^m\|_2^q \right)^{\frac{2}{q}},$$

Final Optimization problem

$$\min_{\substack{w_1, w_2, \dots, w_L, \beta \\ \beta \in \mathbf{R}^M, \beta \geq 0, \|\beta\|_p \leq 1}} \left(\sum_{i=1}^n \ell \left(\sum_{m=1}^M \sqrt{\beta_m} \langle w_L^m, f^m(x_i^m) \rangle + b, y_i \right) + \Lambda \sum_{l=1}^L \sum_{m=1}^M \|w_l^m\|_2^2 \right)$$

$$\min_{w_1, w_2, \dots, w_L} \sum_{i=1}^n \ell \left(\sum_{m=1}^M \langle w_L^m, f^m(x_i^m) \rangle + b, y_i \right) + \Lambda \sum_{l=1}^{L-1} \sum_{m=1}^M \|w_l^m\|_2^2 + \Lambda \left(\sum_{m=1}^M \|w_L^m\|_2^q \right)^{\frac{2}{q}},$$

$$\beta_m = \frac{\|w_l^m\|_2^{\frac{2}{p+1}}}{\left(\sum_{\tilde{m}=1}^M \|w_l^{\tilde{m}}\|_2^{\frac{2p}{p+1}} \right)^{\frac{1}{p}}}$$



Tensor fusion

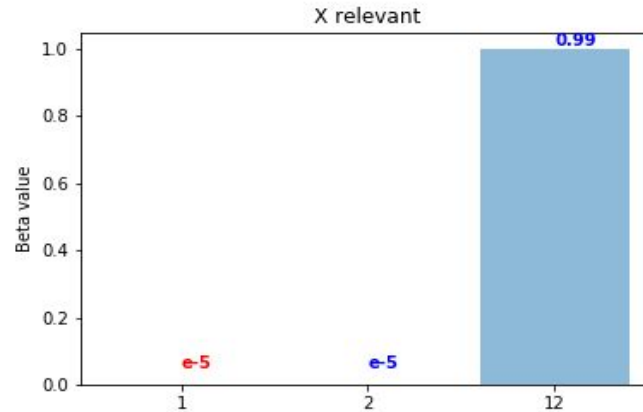
To allow interaction between modalities - take tensor product between modalities.

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \otimes \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} = \begin{bmatrix} a \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} & b \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} \\ c \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} & d \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} \end{bmatrix}$$
$$= \begin{bmatrix} aa^* & ac^* & ba^* & bc^* \\ ab^* & ad^* & bb^* & bd^* \\ ca^* & cc^* & da^* & dc^* \\ cb^* & cd^* & db^* & dd^* \end{bmatrix}$$



Problem with interpretability and tensorfusion - Degree Inflation

Beta weights came to be higher for higher dimension weights - Always high for tensor fusion.





Degree Inflation - reason

When one modality learns constant features.

The information from the first modality can be expressed in the tensorfusion.

Relevant source-with information

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \otimes \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} = \begin{bmatrix} a \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} & b \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} \\ c \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} & d \begin{bmatrix} a^* & c^* \\ b^* & d^* \end{bmatrix} \end{bmatrix}$$
$$= \begin{bmatrix} aa^* & ac^* & ba^* & bc^* \\ ab^* & ad^* & bb^* & bd^* \\ ca^* & cc^* & da^* & dc^* \\ cb^* & cd^* & db^* & dd^* \end{bmatrix}$$

Irrelevant
source-constant



Iterative batch normalisation

We derived a batch norm which does not allow the lower dimension information to be represented in higher dimension(TensorFusion).

This method **helps to remove noise** from the data and give **better accuracies**.



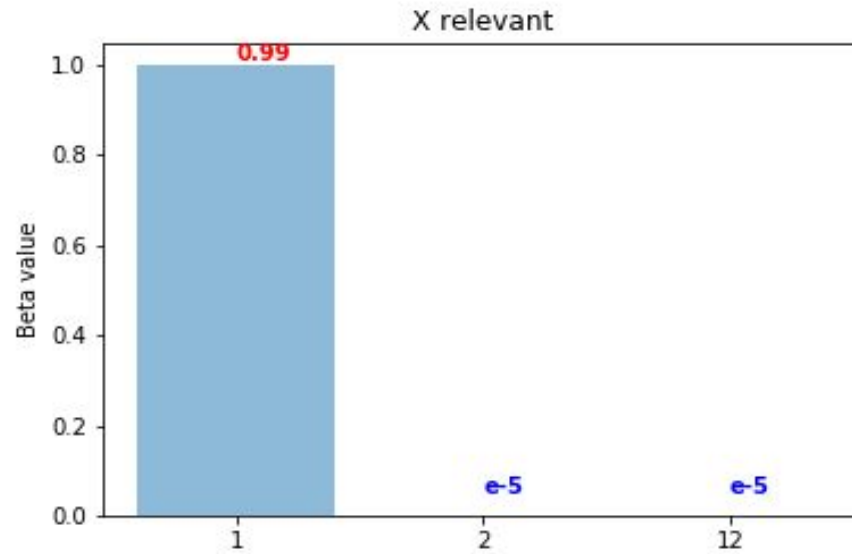
Synthetic data experiment

- Relevant data - Sequences of length 100 (composed of 4 letters - ATGC) with a signature which defines the label

- Irrelevant data - Random 100 length sequences



Example - 1 as relevant source





Thank You